## Monday, November 19, 2012

Agenda:

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- TISK Problems & 2 MM
- Homework Check/Discuss
- Lesson 6-3: Rectangles
- Homework: Finish packet (due 11/27)

TISK Problems  
1) Factor: 
$$15x^2 + 22x + 8$$
  
2) Simplify:  $4y - \frac{18y+6}{3}$   
3) If  $DE = 12$ , what is the distance from A to D?



# Homework Check

6. Yes; you can use the  $\cong$ Supplements Theorem to show  $\angle 1 \cong \angle 2$ , then opp.  $\angle s$  are  $\cong \therefore$  it's a parallelogram.



- 7. Yes; one pair of opp. sides is both  $\cong$  and  $\| \therefore$  it's a  $\|$ ogram
- 8. No; not enough information given.

9. 
$$x = -2$$
 or 3;  $y = \pm 7$ 

10. 
$$x = 64; y = 23.5$$

### Homework Check

Statement	Reason	
$I) \angle A \cong \angle C; \angle B \cong \angle D$	I) Given	
2) $m \angle A + m + x = 180; m \angle C + n + y = 180;$	2) $\Delta$ Sum Th.	
3) $m \angle A = m \angle C, m \angle B = m \angle D$	3) Def. ≅ ∠s	
4) $m \angle B = m + n; m \angle D = x + y$	4) ∠ + Post.	
5) $m \angle A + m + x + m \angle C + n + y = 360$	5) Addition Prop of =	
6) $m \angle A + m \angle B + m \angle C + m \angle D = 360$	6) Substitution Prop of =	
7) $2m \angle A + 2m \angle B = 360;$ $2m \angle B + 2m \angle C = 360$	7) Substitution Prop of =	
8) $m \angle A + m \angle B = 180; m \angle B + m \angle C = 180$	8) Division Prop of =	
9) $\angle A$ and $\angle C$ are supp. to $\angle B$	9) Def. Supp. ∠s	
10) ABCD is a parallelogram	10) Def. parallelogram	

## Homework Check

Statement	Reason	
I) ABCDEF is a regular hexagon	I) Given	
<b>2</b> ) $\overline{AF} \cong \overline{CD}, \overline{AB} \cong \overline{BC}, \overline{ED} \cong \overline{EF}$	2) Def. regular hexagon	
3) $\angle B \cong \angle E$	3) Def. regular hexagon	
$4) \ \Delta ABC \cong \Delta DEF$	4) SAS Post.	
<b>5</b> ) $\overline{AC} \cong \overline{DF}$	5) CPCTC	
6) FDCA is a parallelogram	6) If opp. sides are ≅⇒ it is a ∥ogram	



#### §6.3 Rectangles

- Definition
  - Rectangle
    - A parallelogram is a rectangle if and only if it has 4 congruent angles.

#### Example. Using rectangle properties.

In the diagram, *EFGH* is a rectangle. What is the value of *y*?



All four angles of a rectangle are <u>right angles</u>. So,  $m \angle G = 90^{\circ}$ .

 $(7y + 6)^{\circ} = 90^{\circ}$  Write equation.

7y = 84 Subtract 6 from each side.

y = 12 Divide each side by 7.



#### Theorems

A parallelogram is a rectangle if and only if its diagonals are <u>congruent</u>.

 $BD \cong \overline{AC}$ .



# How do you check to see if a quadrilateral is a rectangle?

- First check to see if it is a parallelogram:
  - Opposite sides are parallel.
  - Opposite sides are congruent.
  - Opposite angles are congruent.
  - Diagonals bisect each other.
  - One pair of opposite sides are both congruent and parallel.
- Then, check to see if it's a rectangle.
  - All 4 angles are right angles.
  - Diagonals are congruent.

# Example. Decide whether the statement is true or false. Explain your reasoning.

• If a quadrilateral has opposite sides that are congruent, then it is a rectangle.

False; a quadrilateral with opposite sides congruent only proves it is a parallelogram, not necessarily a rectangle.

# Example. Determine if the vertices form a rectangle.

- A(-3, I)
- B(4, 8)
- C(7, 5)
- D(0, -2)